

More bits, circuits, adders (From the last class)

CS 2130: Computer Systems and Organization 1

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Assistant Professor

Announcements

- Homework 1 due Monday

Adder

Can we use this in parallel to add multi-bit numbers?

What is missing?

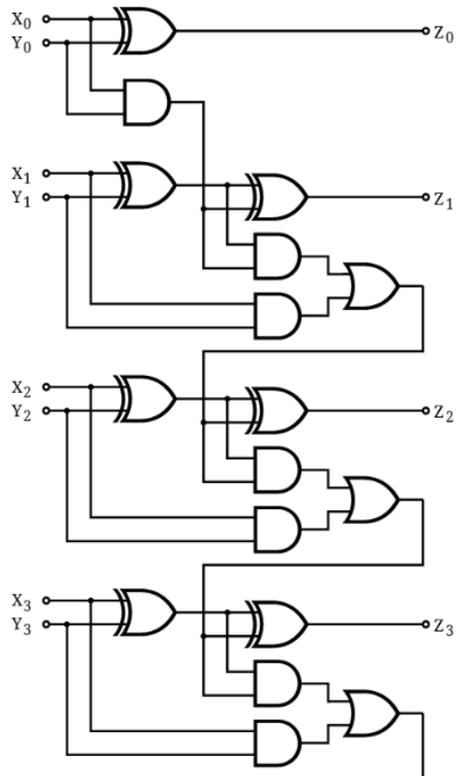
Consider:

$$\begin{array}{r} 11 \\ +01 \\ \hline \end{array}$$

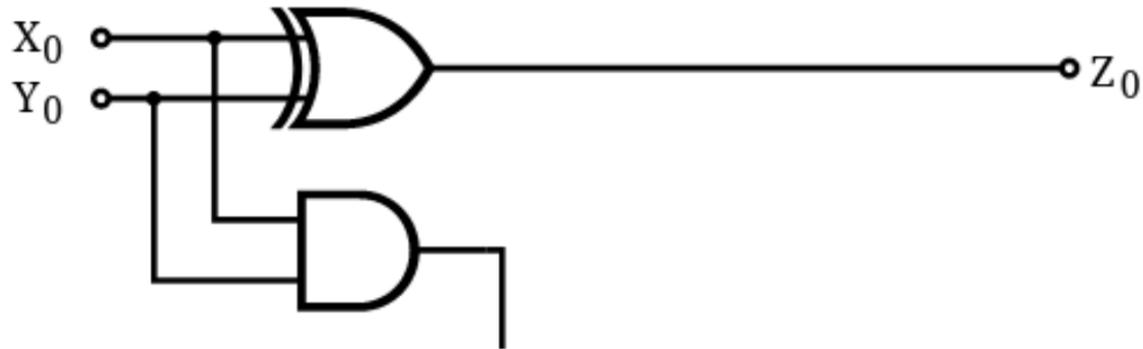
3-input Adder

Add 3 1-bit numbers: a , b , c

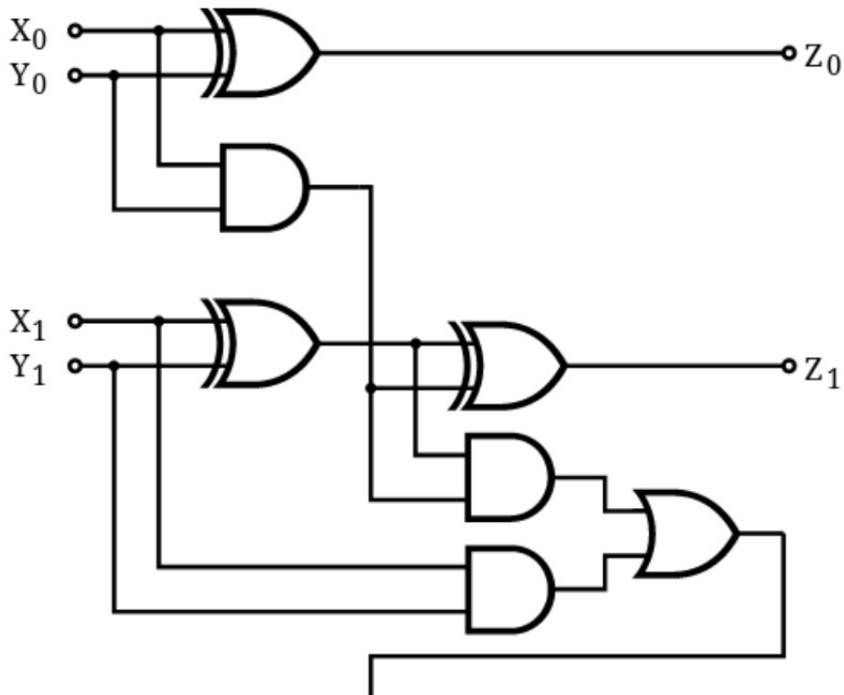
Ripple-Carry Adder



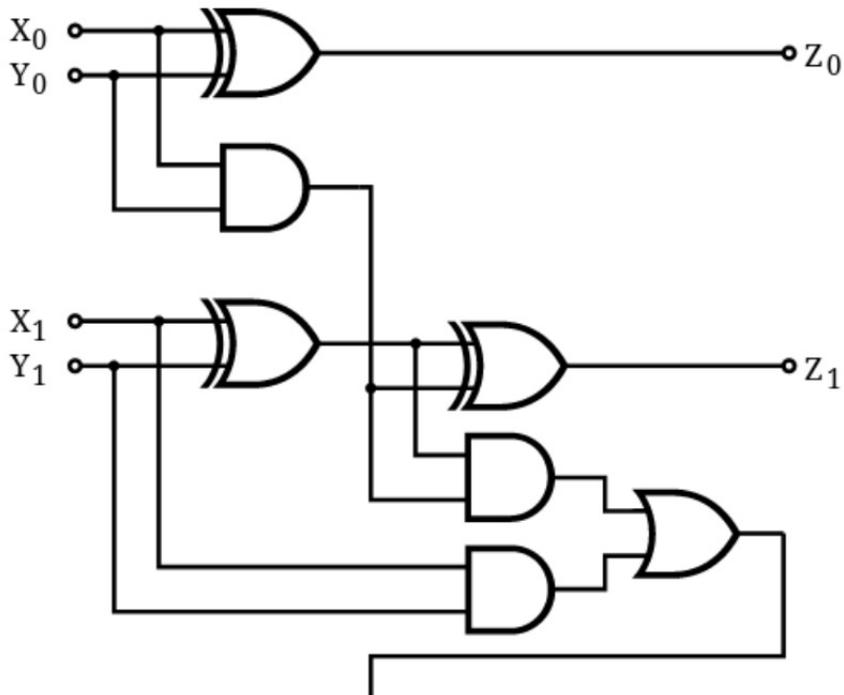
Ripple-Carry Adder: Lowest-order Bit



Ripple-Carry Adder: In General



Ripple-Carry Adder: In General

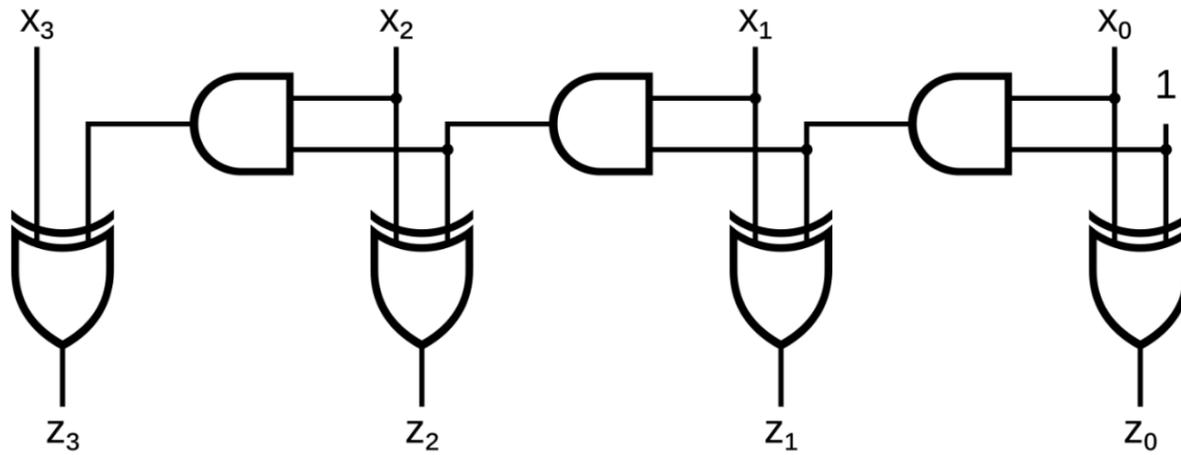


Clocks, Registers

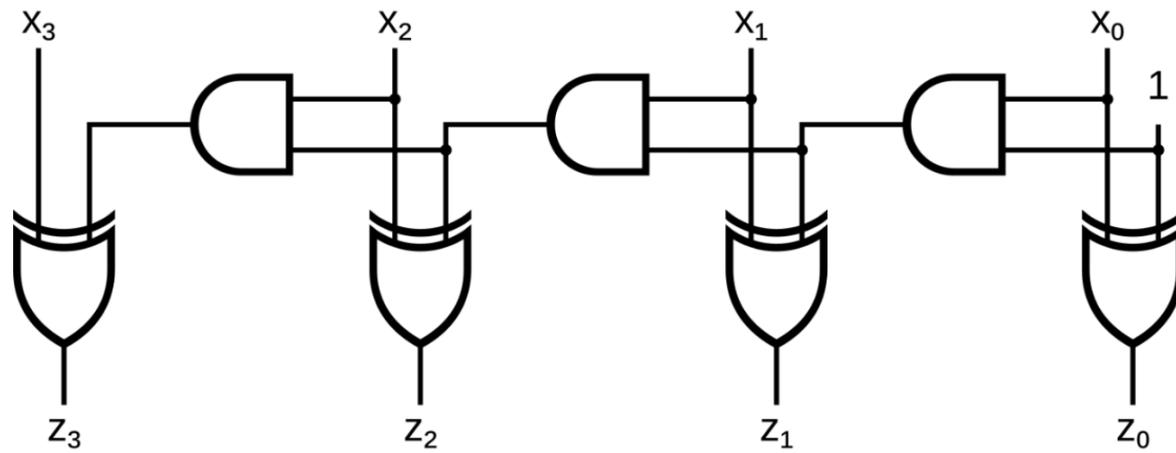
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What does this circuit do?

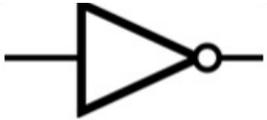


Increment Circuit



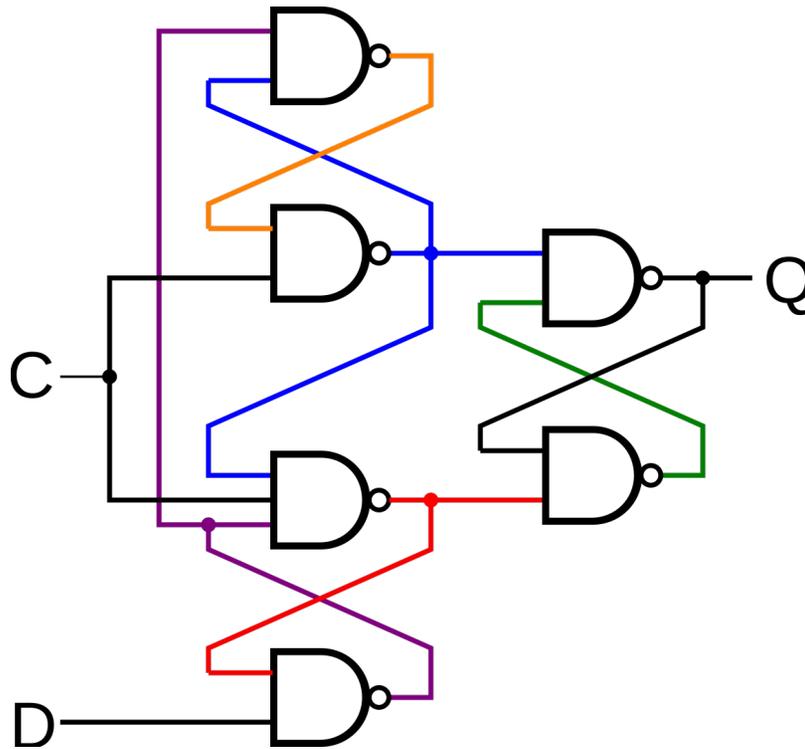
Gate Delay

What happens when I change my input?

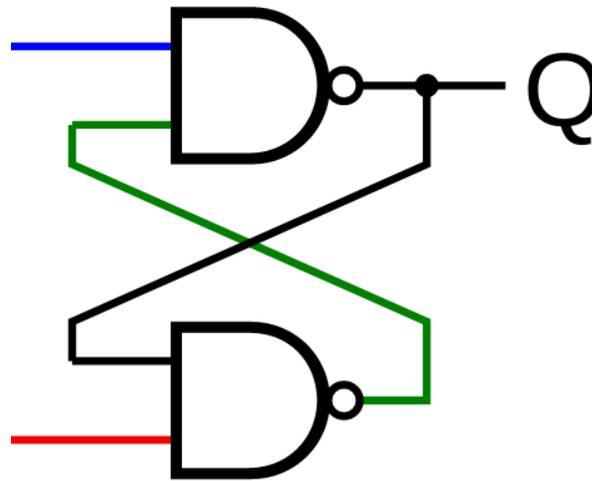


Building a Counter

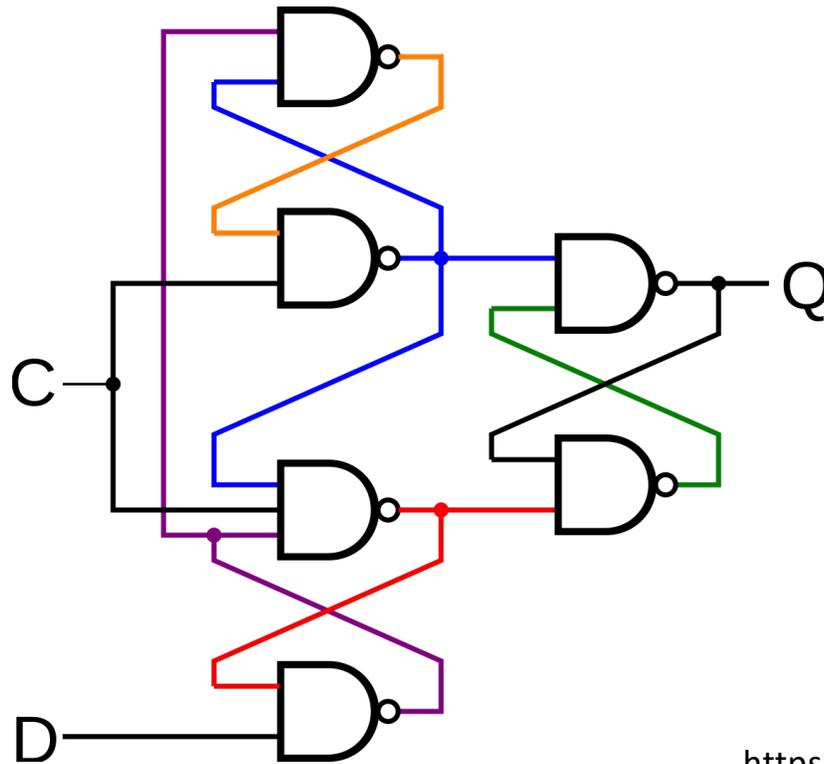
1-bit Register Circuit



1-bit Register Circuit



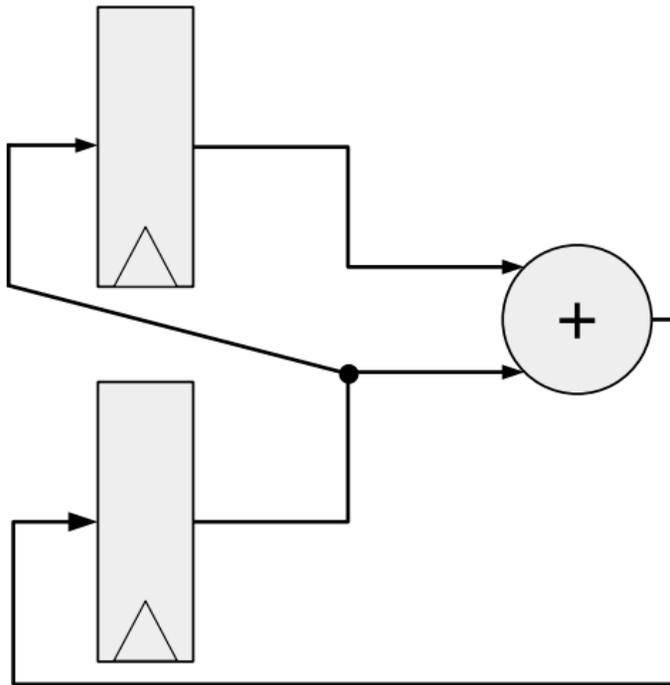
1-bit Register Circuit



<https://www.falstad.com/circuit/e-edgedff.html>

Building a Counter

Another Counter



Common Model in Computers

Code to Build Circuits from Gates

Write code to build circuits from gates

- Gates we already know: $\&$, $|$, \wedge , \sim
- Operations we can build from gates: $+$, $-$
- Others we can build:

Code to Build Circuits from Gates

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- Gates we already know: $\&$, $|$, \wedge , \sim
- Operations we can build from gates: $+$, $-$
- Others we can build:
- Ternary operator: $? :$

Equals

Equals: =

- Attach with a wire (i.e., connect things)
- Ex: $z = x * y$

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$$x = 1$$

$$x = 0$$

Equals

Equals: =

- Attach with a wire (i.e., connect things)
- Ex: $z = x * y$
- What about the following?
 $x = 1$
 $x = 0$
- **Single assignment:** each variable can only be assigned a value once

Subtraction

$$z = x + \sim y + 1$$

$$a = \sim y$$

$$b = a + 1$$

$$z = x + b$$

Comparisons

Each of our comparisons in code are straightforward to build:

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- `!=` - same as `==` without not of output
- `<` - consider $x < 0$
- `>`, `<=`, `=>` are similar

Any Questions?