



Circuits and Code

CS 2130: Computer Systems and Organization 1
September 15, 2025

Announcements

- Homework 1 due tonight
- Homework 2 available today, due next Monday

$$31 = 0 \quad \dots \quad 0 \quad 1 \quad 1 \quad 1 \quad 1 \quad 1$$

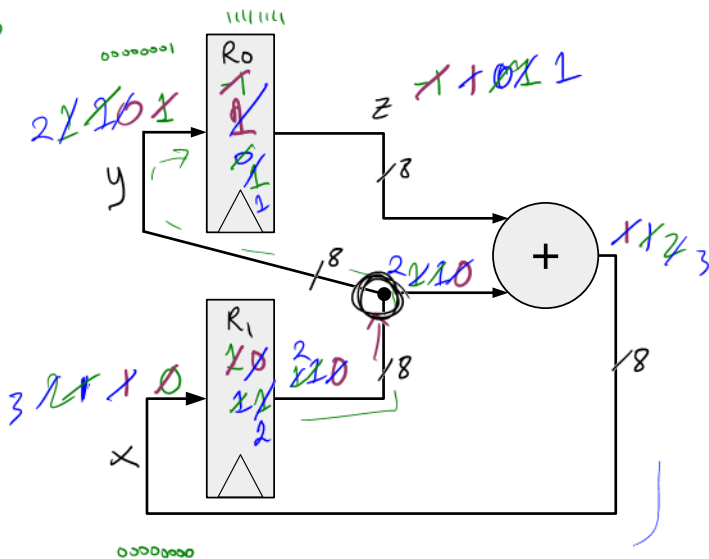
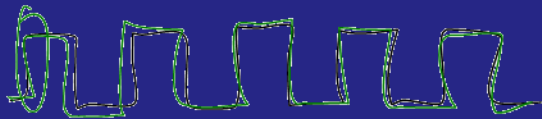
32 16 8 4 2 1

$$a = 000 \dots \dots \quad 01 \quad \ll 31$$

$$c = \underline{1}00 \dots \dots \quad -0 \quad \gg 31$$

$$\quad \quad \underline{1}11 \dots \dots \quad \quad \quad 1$$

Another Circuit



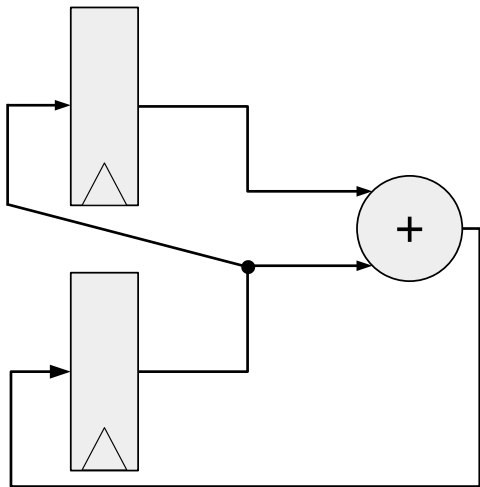
step	x	y	z	R_0	R_1
0	0	1	-1	-1	1
1	1	0	1	1	0
2	1	1	0	0	1
3	2	1	1	1	1
4	3	2	1	1	2

fibonacci

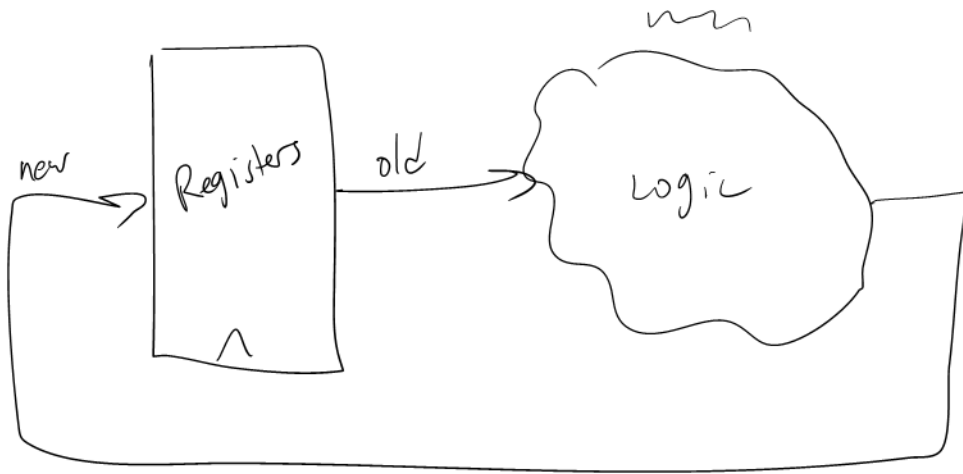
$$y = x$$

$$x = (x+y) + y$$

Another Circuit



Common Model in Computers



Code to Build Circuits from Gates

Write code to build circuits from gates

- Gates we *already* know: $\&$, $|$, \wedge , \sim
- Operations we can build from gates: $+$, $-$
- Others we can build: \times



Hand-drawn binary multiplication:

$$\begin{array}{r} 2130 \\ \times 1101 \\ \hline 2130 \\ 0000 \\ 21300 \\ +213000 \\ \hline \end{array}$$

Annotations: A green arrow points from the multiplier '1' in the second row to the result '2130' in the first row. A blue circle highlights the '+' sign in the fourth row. A blue circle highlights the '000' in the fourth row. A blue double arrow points from the result of the addition to the right.

$/$, $\%$

Code to Build Circuits from Gates

Write code to build circuits from gates

- Gates we *already* know: $\&$, $|$, \wedge , \sim
- Operations we can build from gates: $+$, $-$
- Others we can build:
- Ternary operator: $? :$

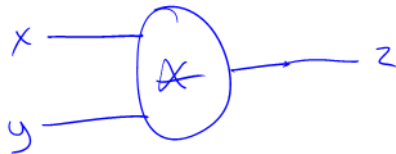
$$z = a ? b : c$$

$$w = (a \implies b ? 32 : y) * x$$

Equals

Equals: =

- Attach with a wire (i.e., connect things)
- Ex: $z = \underline{x * y}$



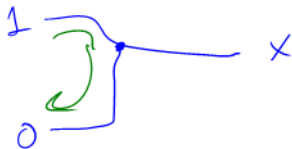
Equals

Equals: =

- Attach with a wire (i.e., connect things)
- Ex: $z = x * y$
- What about the following?

$x = 1$

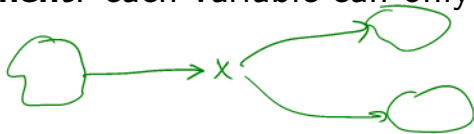
$x = 0$



Equals

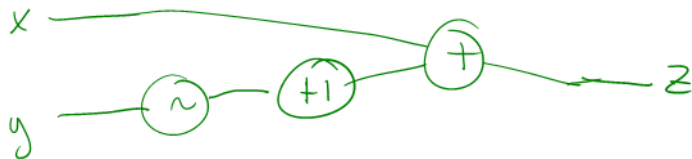
Equals: =

- Attach with a wire (i.e., connect things)
- Ex: $z = x * y$
- What about the following?
 $x = 1$
 $x = 0$
- **Single assignment:** each variable can only be assigned a value once

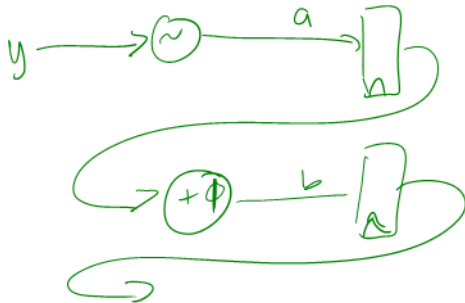


Subtraction

$$z = x + \sim y + 1$$



$$\begin{aligned} a &= \sim y \\ b &= a + 1 \\ z &= x + y \end{aligned}$$



Comparisons

Each of our comparisons in code are straightforward to build:

- == - xor then nor bits of output

Comparisons

Each of our comparisons in code are straightforward to build:

- `==` - xor then nor bits of output
- `!=` - same as `==` without not of output

Comparisons

Each of our comparisons in code are straightforward to build:

- `==` - xor then nor bits of output
- `!=` - same as `==` without not of output
- `<` - consider $x < 0$

Comparisons

Each of our comparisons in code are straightforward to build:

- `==` - xor then nor bits of output
- `!=` - same as `==` without not of output
- `<` - consider $x < 0$
- `>`, `<=`, `=>` are similar

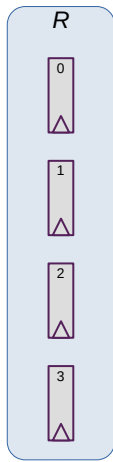
Indexing

Indexing with square brackets: []

- **Register bank** (or **register file**) - an array of registers
 - Can programmatically pick one based on index
 - I.e., can determine which register while running
- Two important operations:
 - $x = R[i]$ - Read from a register
 - $R[j] = y$ - Write to a register

Reading

$x = R[i]$ - connect output of registers to x based on index i

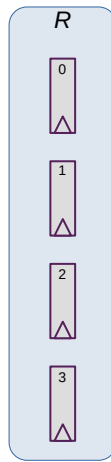


Aside: 4-input Mux

How do we build a 4-input mux? How many wires should i be?

Writing

$R[j] = y$ - connect y to input of registers based on index j



Aside: Creating $==0$ gates

How do we build gates that check for $j == w$?

Need one more thing to build computers

Memory and Storage

Registers

\approx KiB

- 6 gates each, \approx 24 transistors
- Efficient, fast
- Expensive!
- Ex: local variables

These do not persist between power cycles

Memory and Storage

Memory

≈ GiB

- Two main types: SRAM, DRAM
- DRAM: 1 transistor, 1 capacitor per bit
- DRAM is cheaper, simpler to build
- Ex: data structures, local variables

These do not persist between power cycles

Memory and Storage

Disk

≈ GiB-TiB

- Two main types: flash (solid state), magnetic disk
- Magnetic drive
 - Platter with physical arm above and below
 - Cheap to build
 - Very slow! Physically move arm while disk spins
- Ex: files

Data on disk does persist between power cycles

Putting it all together
Next time!