# Boolean Algebra

CS 2130: Computer Systems and Organization 1 August 29, 2025

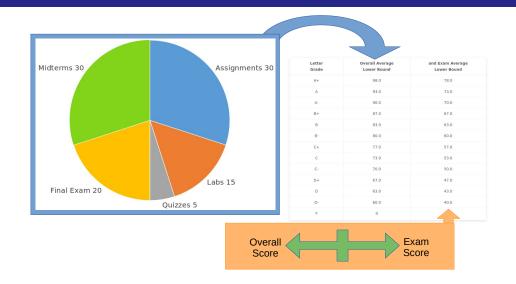
#### **Announcements**

If you need to switch labs:

- Form will be coming soon
- Must be justified (i.e. class conflicts)
- Very limited space to make swaps

Quiz 0 opens tonight, due Sunday 11:59pm

## Measuring Learning: Grading



Boolean Algebra

#### Professionalism, Academic Integrity

#### Honesty

- No plagiarism: cite any and every source you consult (even GenAl)
- Write your own code: Compose it yourself
  - Programming to help learn the content and demonstrate knowledge
  - Unlike industry, in which programming to create product
  - We are looking to cultivate our minds

#### Professionalism, Academic Integrity

#### Honesty

- Working with others is not okay (by default)
- Asking Generative AI to solve your assignments is not okay (by default)
- Do not share your code (even if you are just trying to help)

Consequences of dishonesty are outlined in our Syllabus

#### Generative AI / LLMs

LLMs are great! Generative AI is the future! But...

- Expert generative AI use requires expertise
- We need the background knowledge to guide our use of Gen AI

Guidance for this class

- Do NOT use it to solve homework or generate answers
  - The problem-solving struggle is a good struggle for learning
- Do use it for context, extra practice problems, cleaning up grammar, wordsmithing your (own) answers

#### **Expectations and Evaluations**

#### Illness Policies

- Attendance is not required in lecture, but course engagement is!
  - Watch lecture videos
  - Discuss on Piazza
  - Practice in Lab
- If you don't feel well, stay home, it will be okay
  - Will work with you-if you stay home-to ensure no effect to grade
- Masks are always welcome in class

#### **Editors**

#### Editors and Writing Code

- Familiarity with the command line is a goal of this course
- Setup and practice in Lab 1 and future labs
- You may **not** use online compilers or editors
  - Using an online compiler will result in a 0 on that assignment
- We will **not** be using VSCode until later
- We will ask you to run your code on the CS portal

#### This is a Large Class

How can you get your questions answered?

- Piazza (!!)
  - If you know an answer to someone else's question, answer it!
  - We're in it together for the next semester
  - But remember: do NOT share code or solutions
- TAs (office hours and labs)
- My office hours

#### This is a Large Class

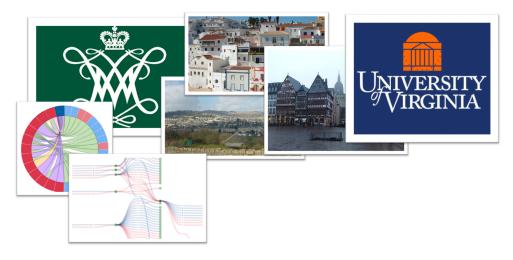
How can you get your questions answered?

- Course email: cs2130@cshelpdesk.atlassian.net
  - Instructors and senior course staff
  - Likely fastest response for direct/personal issues
- My email: jh2jf@virginia.edu
  - Include "CSO1" in the subject
  - Response within a few days

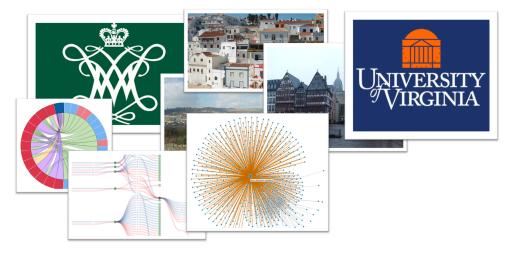


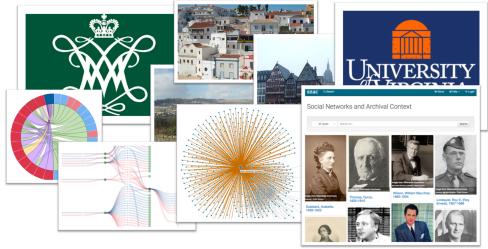






Boolean Algebra





#### **Questions?**

Ask me *almost* anything

Where to start?

Where to start?

0 and 1

#### Why only 0 and 1?

#### Claude Shannon



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## Why only 0 and 1?

#### Vocabulary

- **bit** either a 0 or 1
- binary a system that has only two positions
- trinary a system that has only three positions
- quadrinary a system that has only four positions
- **.**..

#### Vocabulary

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- ...
- decinary ...

#### Vocabulary

- **bit** either a 0 or 1
- binary a system that has only two positions
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- ..

• decimal - system that has ten positions

## Boolean Algebra

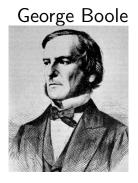


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#### Putting it together

#### Overall idea:

- Only need two things (Shannon)
- We can do math with two things (Boole)

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Now we need a physical device that deals in two levels

## More Vocabulary

Electricity (conceptually) - involves flow of electrons or other charged carriers through a conductive material

- current rate of flow
- voltage pressure of flow

Examples in water

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Examples in water

High pressure, low flow - squirt gun

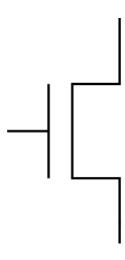
## More Vocabulary

Electricity (conceptually) - involves flow of electrons or other charged carriers through a conductive material

- current rate of flow
- **voltage** pressure of flow

Examples in water

- High pressure, low flow squirt gun
- Low pressure, high flow bucket of water

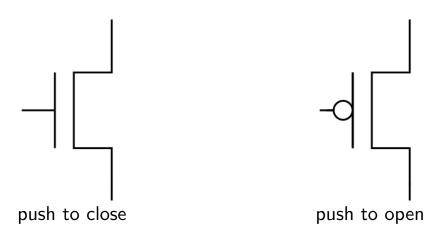


Transistors act like an electrically-triggered switch

- No voltage, no current
- Apply voltage to allow current to flow

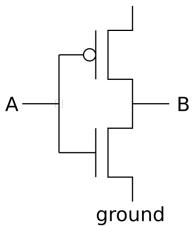
#### Transistors act like an electrically-triggered switch

- No voltage, no current
- Apply voltage to allow current to flow
- The amount of voltage needed to close the gate is boundary between 0 and 1
- Central technique for how we are going to build binary computers

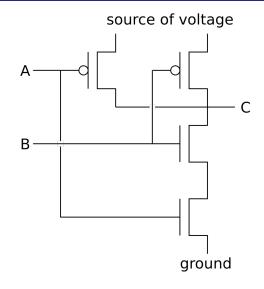


## **Circuit Diagram**

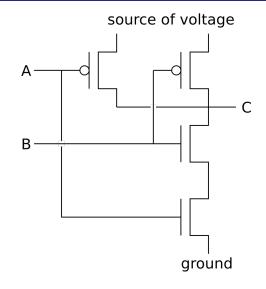
#### source of voltage



## **Circuit Diagram**



## **Circuit Diagram**



Other Gates (reading)

### **Building Up**

#### Where we are now

- World with only 2 states: 0 and 1
- Re-developed Boolean logic: and, or, not

Gives us everything Boole talked about

- We can do a lot of interesting things!
- Next: build higher level ideas: the trinary operator

### Trinary Operator

### General idea

```
if ( ... ) {
    ...
} else {
    ...
}
```

Trinary operator (expression if)

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Python: x = b if a else c

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### General idea

```
if ( ... ) {
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```

Trinary operator (expression if)

- Python: x = b if a else c
- Java: x = a ? b : c

# Multiplexer (mux)

$$x = a ? b : c$$

## Multiplexer (mux)

How can we build a mux out of what we have learned so far? x = a? b : c

### Multiplexer (mux)

Can be built from and, or, and not

- Can be built using transistors
- Can physically put it in silicon!

Mux will be the key when constructing a computer out of gates and circuits!

Questions?

More bits!

# 2-bit Multiplexer (mux)

2-bit values instead of 1-bit values