DUE FRIDAY, APRIL 15, 2022 AT 11:30 pm VIA GRADESCOPE

## С2 basic $^{\text {(MSTЗК) }}$

Collaboration Policy: You are encouraged to collaborate with up to 3 other students, but all work submitted must be your own independently written solution. List the computing ids of all of your collaborators in the collabs command at the top of the tex file. Do not share written notes, documents (including Google docs, Overleaf docs, discussion notes, PDFs), or code. Do not seek published or online solutions for any assignments. If you use any published or online resources (which may not include solutions) when completing this assignment, be sure to cite by naming the book etc. or listing a website's URL. Do not submit a solution that you are unable to explain orally to a member of the course staff. Any solutions that share similar text/code will be considered in breach of this policy. Please refer to the syllabus for a complete description of the collaboration policy.

Collaborators: list collaborators's computing IDs
Sources: Cormen, et al, Introduction to Algorithms. (add others here)

## problem 1 Load Balancing

You work for a print shop with 4 printers. Each printer $i$ has a queue with $n$ jobs: $j_{i, 1}, \ldots, j_{i, n}$. Each job has a number of pages, $p\left(j_{i, m}\right)$. A printer's workload $W_{i}=\sum_{\ell} p\left(j_{i, \ell}\right)$ is the sum of all pages across jobs for for that printer. Your goal is to equalize the workload across all 4 printers so that they all print the same number of total pages. You may only remove jobs from the end of their queues, i.e., job $j_{i, n}$ must be removed before job $j_{i, n-1}$, and you are allowed to remove a different number of jobs from each printer. Give a greedy algorithm to determine the maximum equalized workload (possibly 0 pages) across all printers. Be sure to state your greedy choice property.

Solution: Your answer here!
problem 2 Short Answer Questions. (You don't have to explain your answers in your submission, but you should understand the reason behind your answer.)
A. True or false? Issuing the largest coin first will always solve the coin change problem if only two coins are available: the penny and one larger coin. Assume the amount of change is $\geq$ the larger coin.
Solution: Your answer here!
B. True or false? The interval scheduling problem is always guaranteed to have an optimal solution that contains the interval with the earliest finish time.
Solution: Your answer here!
C. Choose one: In our proof of the correctness of the greedy solution to the interval scheduling problem, we exchanged the interval $i$ selected by our greedy choice with another interval that finished earlier/later than interval $i$. (Your answer is one of "earlier" or "later.")
Solution: Your answer here!
D. True or false? A feasible solution for the Huffman encoding problem is any valid prefix-free code-word table $T$.
Solution: Your answer here!

## problem 3 Optimal Substructure

Please answer the following questions related to Optimal Substructure.
A. What's the difference in how dynamic programming algorithms versus greedy algorithms use optimal substructure?

Solution: Your answer here!
B. Why did we need to prove the optimal substructure for our greedy Huffman coding algorithm?

Solution: Your answer here!
problem 4 Gradescope Submission
Submit a version of this .tex file to Gradescope with your solutions added, along with the compiled PDF. You should only submit your .pdf and .tex files.

